

Sine (sin) / Cosine (cos) / Tangent (tan)

To remember the trigonometric ratio we can use the following saying:

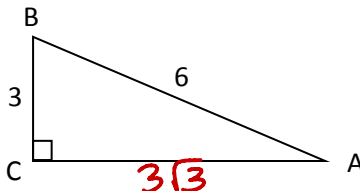
SOH-CAH-TOA

Sin = $\frac{\text{opposite}}{\text{hypotenuse}}$

Cos = $\frac{\text{adjacent}}{\text{hypotenuse}}$

Tan = $\frac{\text{opposite}}{\text{adjacent}}$

1. Using the triangle below express sine-cosine-tangent.

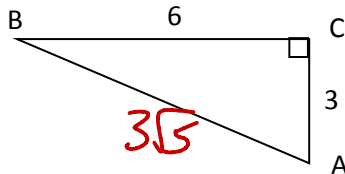


$3^2 + b^2 = 6^2$
 $9 + b^2 = 36$
 $b^2 = 27$
 $b = \sqrt{27}$
 $b = 3\sqrt{3}$

$\sin A = \frac{3}{6} = \frac{1}{2}$
 $\cos A = \frac{3\sqrt{3}}{6} = \frac{\sqrt{3}}{2}$
 $\tan A = \frac{3}{3\sqrt{3}} = \frac{1}{\sqrt{3}} = \frac{\sqrt{3}}{3}$

$\sin B = \frac{3\sqrt{3}}{6} = \frac{\sqrt{3}}{2}$
 $\cos B = \frac{3}{6} = \frac{1}{2}$
 $\tan B = \frac{3\sqrt{3}}{3} = \sqrt{3}$

2. Using the triangle below express sine-cosine-tangent. NO DECIMALS!



$3^2 + 6^2 = c^2$
 $45 = c^2$
 $\sqrt{45} = c \rightarrow c = 3\sqrt{5}$

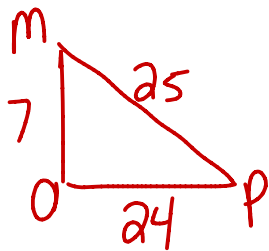
$\sin A = \frac{6}{3\sqrt{5}} = \frac{2}{\sqrt{5}} = \frac{2\sqrt{5}}{5}$
 $\cos A = \frac{3}{3\sqrt{5}} = \frac{1}{\sqrt{5}} = \frac{\sqrt{5}}{5}$
 $\tan A = \frac{6}{3} = 2$

$\sin B = \frac{3}{3\sqrt{5}} = \frac{1}{\sqrt{5}} = \frac{\sqrt{5}}{5}$
 $\cos B = \frac{6}{3\sqrt{5}} = \frac{2}{\sqrt{5}} = \frac{2\sqrt{5}}{5}$
 $\tan B = \frac{3}{6} = \frac{1}{2}$

3. The $\cos 60^\circ$ is $1/2$. What does this mean? Your explanation should include something about the sides of a right triangle.

The side adjacent to the 60° angle is 1 and the hypotenuse is 2.

4. In $\triangle MOP$, $\angle O$ is the right angle. Suppose $\sin P = \frac{7}{25}$. Find $\sin M$ and $\cos P$.



$$7^2 + b^2 = 25^2$$

$$b^2 = 576$$

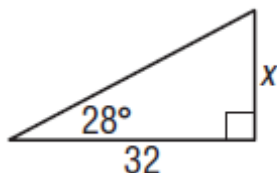
$$b = 24$$

$$\sin M = \frac{24}{25}$$

$$\cos P = \frac{24}{25}$$

Examples: Find the missing side lengths.

10.

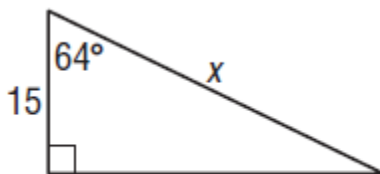


$$\sin 28 = \frac{x}{32}$$

$$x = 32 \sin 28$$

$$x = 15.0$$

11.



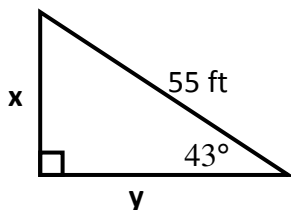
$$\cos 64 = \frac{15}{x}$$

$$x \cos 64 = 15$$

$$x = \frac{15}{\cos 64}$$

$$x = 34.2$$

12.



$$\sin 43 = \frac{x}{55}$$

$$55 \sin 43 = x$$

$$37.51 = x$$

$$\text{ft}$$

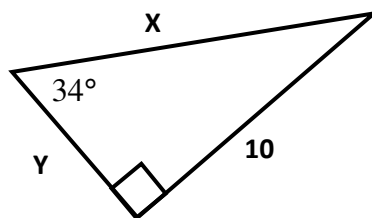
$$\cos 43 = \frac{y}{55}$$

$$55 \cos 43 = y$$

$$40.22 = y$$

$$\text{ft}$$

13.



$$\sin 34 = \frac{10}{x}$$

$$x \sin 34 = 10$$

$$x = \frac{10}{\sin 34} = 17.9$$

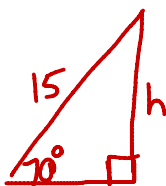
$$\tan 34 = \frac{10}{y}$$

$$y \tan 34 = 10$$

$$y = \frac{10}{\tan 34}$$

$$y = 14.8$$

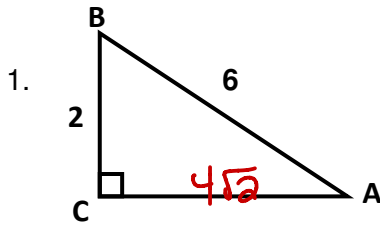
15. A 15-foot ladder leans against a wall. The **angle of elevation** (the angle between the ladder and ground) is 70° . How far up the wall does the ladder reach?



$$\sin 70 = \frac{h}{15}$$

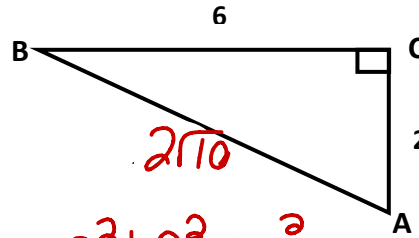
$$15 \sin 70 = h \rightarrow h = 14.1 \text{ ft}$$

Find sin, cos, and tan for each angle in the triangle.



$$\begin{aligned} a^2 + b^2 &= c^2 \\ 4 + b^2 &= 36 \\ b^2 &= 32 \\ b &= 4\sqrt{2} \end{aligned}$$

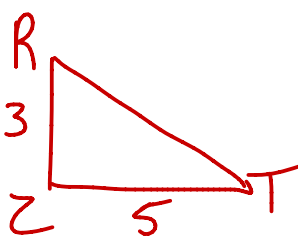
$$\begin{aligned} \sin A &= \frac{2}{6} = \frac{1}{3} & \sin B &= \frac{4\sqrt{2}}{6} = \frac{2\sqrt{2}}{3} \\ \cos A &= \frac{4\sqrt{2}}{6} = \frac{2\sqrt{2}}{3} & \cos B &= \frac{2}{6} = \frac{1}{3} \\ \tan A &= \frac{2}{4\sqrt{2}} = \frac{1}{2\sqrt{2}} = \frac{\sqrt{2}}{4} & \tan B &= \frac{4\sqrt{2}}{2} = 2\sqrt{2} \end{aligned}$$



$$\begin{aligned} 2^2 + 6^2 &= c^2 \\ 40 &= c^2 \\ 2\sqrt{10} &= c \end{aligned}$$

$$\begin{aligned} \sin A &= \frac{6}{2\sqrt{10}} = \frac{3}{\sqrt{10}} = \frac{3\sqrt{10}}{10} & \sin B &= \frac{2}{2\sqrt{10}} = \frac{1}{\sqrt{10}} = \frac{\sqrt{10}}{10} \\ \cos A &= \frac{2}{2\sqrt{10}} = \frac{1}{\sqrt{10}} = \frac{\sqrt{10}}{10} & \cos B &= \frac{6}{2\sqrt{10}} = \frac{3}{\sqrt{10}} = \frac{3\sqrt{10}}{10} \\ \tan A &= \frac{6}{2} = 3 & \tan B &= \frac{2}{6} = \frac{1}{3} \end{aligned}$$

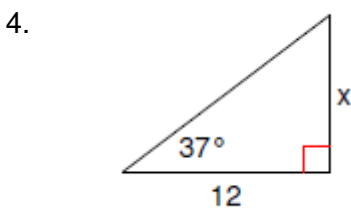
3. In $\triangle RTZ$, $\angle Z$ is the right angle. Suppose $\tan R = \frac{5}{3}$. Find $\cos T$ and $\sin R$.



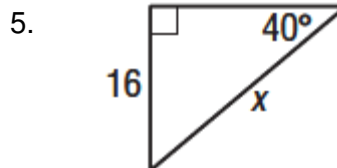
$$\begin{aligned} 5^2 + 3^2 &= c^2 \\ 34 &= c^2 \\ \sqrt{34} &= c \end{aligned}$$

$$\begin{aligned} \cos T &= \frac{5}{\sqrt{34}} = \frac{5\sqrt{34}}{34} \\ \sin R &= \frac{5}{\sqrt{34}} = \frac{5\sqrt{34}}{34} \end{aligned}$$

Find the missing side lengths.



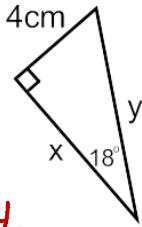
$$\begin{aligned} \tan 37 &= \frac{x}{12} \\ 12 \tan 37 &= x \\ 9.04 &= x \end{aligned}$$



$$\begin{aligned} \sin 40 &= \frac{16}{x} \\ x \sin 40 &= 16 \\ x &= \frac{16}{\sin 40} \\ x &= 24.9 \end{aligned}$$

Find the missing side lengths.

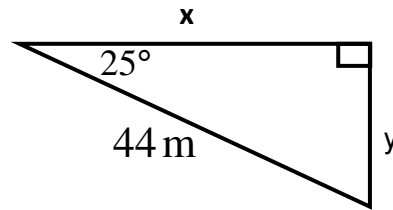
6.



$$\begin{aligned} \tan 18 &= \frac{4}{x} \\ x \tan 18 &= 4 \\ x &= \frac{4}{\tan 18} \\ \boxed{x = 12.31 \text{ cm}} \end{aligned}$$

$$\begin{aligned} \sin 18 &= \frac{4}{y} \\ y \sin 18 &= 4 \\ y &= \frac{4}{\sin 18} \\ \boxed{y = 12.94 \text{ cm}} \end{aligned}$$

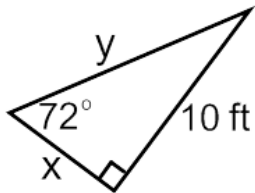
7.



$$\begin{aligned} \sin 25 &= \frac{y}{44} \\ 44 \sin 25 &= y \\ \boxed{18.60 = y} \\ &\text{m} \end{aligned}$$

$$\begin{aligned} \cos 25 &= \frac{x}{44} \\ 44 \cos 25 &= x \\ \boxed{39.88 = x} \\ &\text{m} \end{aligned}$$

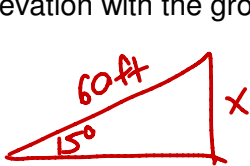
8.



$$\begin{aligned} \tan 72 &= \frac{10}{x} \\ x \tan 72 &= 10 \\ x &= \frac{10}{\tan 72} \\ \boxed{x = 3.25 \text{ ft}} \end{aligned}$$

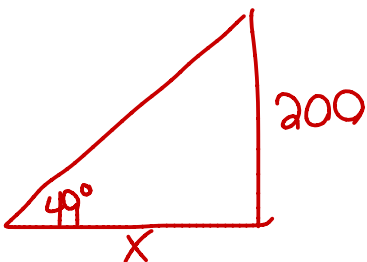
$$\begin{aligned} \sin 72 &= \frac{10}{y} \\ y \sin 72 &= 10 \\ y &= \frac{10}{\sin 72} \\ \boxed{y = 10.51 \text{ ft}} \end{aligned}$$

9. A 60-foot ramp rises from the first floor to the second floor of a parking garage and makes a 15° angle of elevation with the ground. How high above the first floor is the second floor?



$$\begin{aligned} \sin 15 &= \frac{x}{60} \\ 60 \sin 15 &= x \rightarrow \boxed{x = 15.53 \text{ ft}} \end{aligned}$$

10. Sadie is having trouble getting a signal for her cell phone during class, so she decides to leave the class and stand near a 200 foot high cell phone tower. If the angle of elevation from the ground where Sadie is standing to the top of the cell phone tower is 49° , how far from the tower is she standing?



$$\begin{aligned} \tan 49 &= \frac{200}{x} \\ x \tan 49 &= 200 \\ x &= \frac{200}{\tan 49} \\ \boxed{x = 173.86 \text{ ft}} \end{aligned}$$