

Simplify each of the following by performing the indicated operation.

$$1.) \frac{2a^2}{5b^2c} \cdot \frac{3bc^2}{8a^2} = \boxed{\frac{3c}{20b}}$$

$$2.) \frac{y^2}{x+2} \div \frac{y}{x+2} \rightarrow$$

$$= \frac{y^2}{x+2} \cdot \frac{x+2}{y} = \boxed{y}$$

$$3.) \frac{x^{10}y^4}{33x^4} \div \frac{4y^{10}}{39x^5} \rightarrow$$

$$= \frac{x^{10}y^4}{33x^4} \cdot \frac{39x^5}{4y^{10}} = \boxed{\frac{13x^{11}}{4y^6}}$$

$$4.) \frac{c^2-3c}{c^2-25} \cdot \frac{c^2+4c-5}{c^2-4c+3}$$

$$= \frac{c(c-3)}{(c-5)(c+5)} \cdot \frac{(c+5)(c-1)}{(c-1)(c-3)} = \boxed{\frac{c}{c-5}}$$

$$5.) \frac{3x+6}{7x-7} \cdot \frac{14x-14}{2x-2}$$

$$= \frac{3(x+2)}{7(x-1)} \cdot \frac{14(x-1)}{2(x-1)} = \boxed{\frac{3(x+2)}{x-1}}$$

$$6.) \frac{3x^2-3}{2x^2+8x+6} \div \frac{5x^2-10x+5}{4x+12} \rightarrow$$

$$= \frac{3(x-1)(x+1)}{2(x+1)(x+3)} \cdot \frac{4(x+3)}{5(x-1)(x-1)}$$

$$= \boxed{\frac{6}{5(x-1)}}$$

$$7.) \frac{8x^2-72}{5x+10} \cdot \frac{4x-12}{5x}$$

$$= \frac{8(x^2-9)}{5(x+2)} \cdot \frac{4(x-3)}{5x}$$

$$= \frac{8(x-3)(x+3)}{5(x+2)} \cdot \frac{4(x-3)}{5x}$$

$$= \boxed{\frac{x(x+3)}{x+2}}$$

$$8.) \frac{5x^2-5x-30}{45-15x} \cdot \frac{6+x-x^2}{4x-12}$$

$$= \frac{5(x^2-x-6)}{-15(-3+x)} \cdot \frac{-1(x^2-x-6)}{4(x-3)}$$

$$= \frac{5(x-3)(x+2)}{-15(x-3)} \cdot \frac{4(x-3)}{-1(x-3)(x+2)}$$

$$= \boxed{\frac{4}{3}}$$

Simplify each of the following by performing the indicated operation.

$$9.) \frac{x-3}{2x-8} \cdot \frac{6x^2-96}{x^2-9}$$

$\frac{6(x^2-16)}{2(x-4)(x-3)(x+3)}$

$$= \frac{\cancel{x-3}}{2\cancel{x-4}} \cdot \frac{6\cancel{(x-4)}(x+4)}{(x-3)(x+3)} = \boxed{\frac{3(x+4)}{x+3}}$$

$$11.) \frac{2a^2}{8ab^2} \cdot \frac{(a^2+4)(b-3)}{(a-2)(a^2+4)}$$

$\frac{1a}{4}$

$$= \boxed{\frac{a(b-3)}{4b^2(a-2)}}$$

$$13.) \frac{3(2x-1)}{2x+10} \cdot \frac{4(x-1)(x-1)}{12x^2+6x-6}$$

$\frac{4(x-1)(x-1)}{6(2x^2+x-1)}$

$$= \frac{3(2x-1)}{2(x+5)} \cdot \frac{4(x-1)(x-1)}{6(2x-1)(x+1)}$$

$$= \boxed{\frac{(x-1)(x-1)}{(x+5)(x+1)}}$$

$$15.) \frac{x^2+8x+15}{x^2+2-6} \cdot \frac{(x+5)(x+3)}{(x^2-4)}$$

$\frac{(x+5)(x-3)}{(x-3)(x+1)}$

$$= \frac{\cancel{(x+5)}(x+3)}{(x-2)(x+2)} \cdot \frac{(x-3)(x+1)}{\cancel{(x+5)}(x-3)}$$

$$= \boxed{\frac{(x+3)(x+1)}{(x-2)(x+2)}}$$

$$10.) \frac{x(x+3)}{x^2+6x+8} \div \frac{4x^2(x+3)}{x^2+x-2}$$

$\frac{4x^2(x+3)}{(x+2)(x-1)}$

$$= \frac{\cancel{x}(x+3)}{(x+2)(x+4)} \cdot \frac{(x+2)(x-1)}{4\cancel{x^2}(x+3)}$$

$$= \boxed{\frac{x-1}{x(x+4)}}$$

$$12.) \frac{x^2+3x-4}{x^2-4x+3} \cdot \frac{3-x}{x+4} = \frac{(x+4)\cancel{(x-1)}}{(x-3)(x-1)} \cdot \frac{-1(x-3)}{(x+4)}$$

$$= \boxed{-1}$$

$$14.) \frac{5x^2+10x-75}{4x^2-24x-28} \div \frac{x^2+7x+10}{2x^2-10x-28}$$

$\frac{5(x^2+2x-15)}{4(x^2-6x-7)} \cdot \frac{(x+2)(x+5)}{2(x^2-5x-14)}$

$$= \frac{5\cancel{(x+5)}(x-3)}{4\cancel{(x+7)}(x+1)} \cdot \frac{2\cancel{(x-7)}(x+2)}{(x+2)(x+5)}$$

$$= \boxed{\frac{5(x-3)}{2(x+1)}}$$

$$16.) \frac{x^2-100}{x^2} \cdot \frac{(x-10)(x+10)}{x^2}$$

$\frac{3x^2-31x+10}{2x} \cdot \frac{(x-10)(3x-1)}{2x}$

$$= \frac{\cancel{(x-10)}(x+10)}{\cancel{x^2}} \cdot \frac{2x}{(x-10)(3x-1)}$$

$$= \boxed{\frac{2(x+10)}{x(3x-1)}}$$