

Ratios and Proportions

RATIO (RATE): A comparison of 2 numbers by division.

Ways to Write a Ratio (Rate)

- a to b
- $a : b$ where b is not equal to 0.
- $\frac{a}{b}$

UNIT RATE: A rate where $b = 1$ or when the denominator = 1.

Find the unit rate.

1. If you work 6 hours and make a total of \$54, how much do you make per hour?

$$\frac{\$54}{6 \text{ Hours}} = \boxed{\$9/\text{Hour}}$$

2. Mr. Lee gives way too much homework. In the next 4 weeks, he plans to give 524 problems to his Expanded Math classes. How many homework problems is that per week?

$$\frac{524 \text{ PROBLEMS}}{4 \text{ WEEKS}} = \boxed{131 \text{ PROBLEMS/WEEK}}$$

3. A 10-ounce bottle of shampoo costs \$2.40. What is the cost per ounce?

$$\frac{\$2.40}{10 \text{ oz}} = \boxed{\$0.24/\text{oz}}$$

PROPORTIONS: An equation that states 2 ratios are equal.

Determine if the 2 ratios are proportional.

4. $\frac{8}{24} \overset{\times}{\cancel{=}} \frac{16}{48}$

$$24(8) = 8(48)$$

$$384 = 384$$

YES

5. $\frac{5}{10} \overset{\times}{\cancel{=}} \frac{6}{3}$

$$10(6) = 5(3)$$

$$60 = 15$$

NO

6. $\frac{10}{30} \overset{\times}{\cancel{=}} \frac{4}{12}$

$$30(4) = 10(12)$$

$$120 = 120$$

YES

Solve each proportion by finding the value of x .

$$7. \quad \frac{x}{24} \cancel{\times} \frac{1}{3}$$

$$24 = 3x$$

$$\boxed{8 = x}$$

$$8. \quad -\frac{3}{x} \cancel{\neq} \frac{6}{10}$$

$$6x = -3(10)$$

$$6x = -30$$

$$\boxed{x = -5}$$

$$9. \quad \frac{6}{8} \cancel{\neq} \frac{21}{x}$$

$$8(-21) = 6x$$

$$-168 = 6x$$

$$\boxed{-28 = x}$$

$$10. \quad -\frac{5}{8} \cancel{\neq} \frac{7}{x}$$

$$-8(7) = 5x$$

$$-56 = 5x$$

$$\boxed{-11.2 = x}$$

$$11. \quad \frac{2}{1.2} \cancel{\neq} \frac{5}{x}$$

$$1.2(5) = 2x$$

$$6 = 2x$$

$$\boxed{3 = x}$$

$$12. \quad \frac{11}{18} \cancel{\neq} -\frac{x}{49.5}$$

$$18x = 11(-49.5)$$

$$18x = -544.5$$

$$\boxed{x = -30.25}$$

$$13. \quad \frac{(x+2)}{14} \cancel{\neq} \frac{5}{10}$$

$$14(5) = 10(x+2)$$

$$70 = 10x + 20$$

$$50 = 10x$$

$$\boxed{5 = x}$$

$$14. \quad \frac{9x}{(x+12)} \cancel{\neq} \frac{9}{5}$$

$$9(x+12) = 5(9x)$$

$$9x + 108 = 45x$$

$$108 = 36x$$

$$\boxed{3 = x}$$

$$15. \quad \frac{(18+x)}{3} \cancel{\neq} \frac{(14-x)}{7}$$

$$3(14-x) = 7(18+x)$$

$$42 - 3x = 126 + 7x$$

$$-84 = 10x$$

$$\boxed{-8.4 = x}$$

$$16. \quad \frac{(2x-2)}{14} \cancel{\neq} \frac{(2x-4)}{6}$$

$$14(2x-4) = 6(2x-2)$$

$$28x - 56 = 12x - 12$$

$$14x = 44$$

$$\boxed{x = 2.75}$$

$$17. \quad \frac{6}{(x+2)} \cancel{\neq} \frac{12}{(x-1)}$$

$$12(x+2) = 6(x-1)$$

$$12x + 24 = 6x - 6$$

$$6x = -30$$

$$\boxed{x = -5}$$

$$18. \quad -\frac{(x+8)}{10} \cancel{\neq} \frac{(x-3)}{2}$$

$$-2(x+8) = -10(x-3)$$

$$-2x - 16 = -10x + 30$$

$$8x = 46$$

$$\boxed{x = 5.75}$$