

What is a System of Equations?

A set of two or more equations with the same variable.

What is a Solution to a System of Equations?

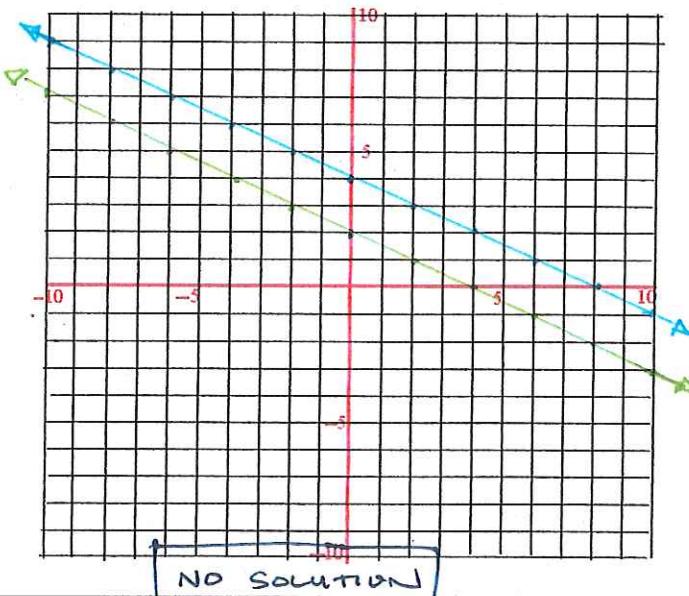
A set of values for the variables that satisfy all the equations simultaneously.

What does a Solution do for a System of Equations?

Defines the possible types of solutions: NO solution (lines do not intersect), ONE solution (point where lines intersect), or INFINITELY MANY SOLUTIONS (same line).

Solve.

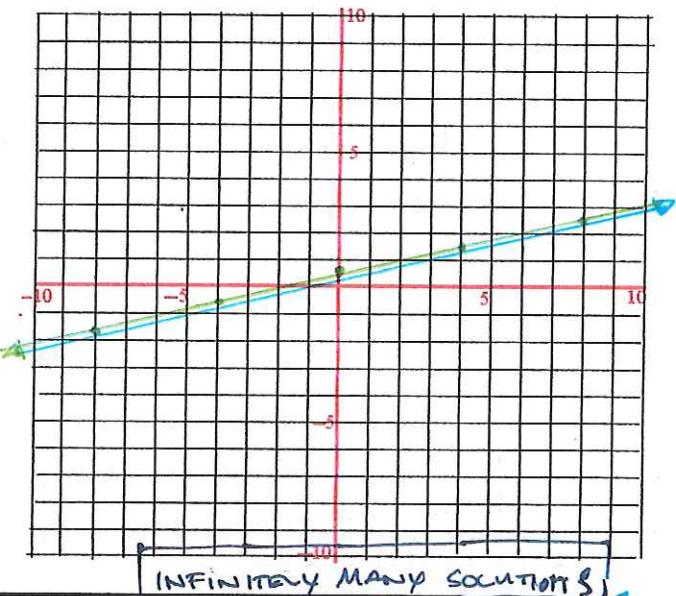
$$\begin{aligned} 1.) \quad & 3x + 6y - 12 = 0 \rightarrow y = -\frac{1}{2}x + 2 \\ & x + 2y = 8 \rightarrow y = -\frac{1}{2}x + 4 \end{aligned}$$



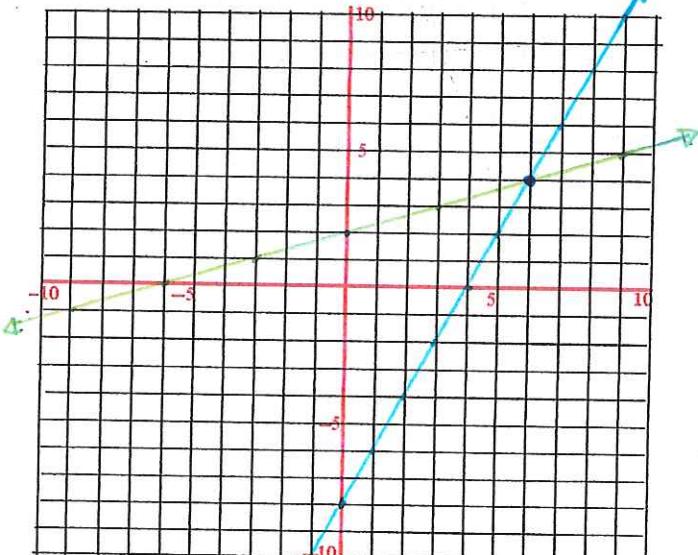
$$\begin{aligned} 3.) \quad & -x + 3y = 6 \rightarrow y = \frac{1}{3}x + 2 \\ & 2x - y = 8 \rightarrow y = 2x + 8 \end{aligned}$$

1 solution
(6, 4)

$$\begin{aligned} 2.) \quad & 3 = 4y + x \rightarrow y = -\frac{1}{4}x + \frac{3}{4} \\ & 8y = -2x + 6 \rightarrow y = -\frac{1}{4}x + \frac{3}{4} \end{aligned}$$

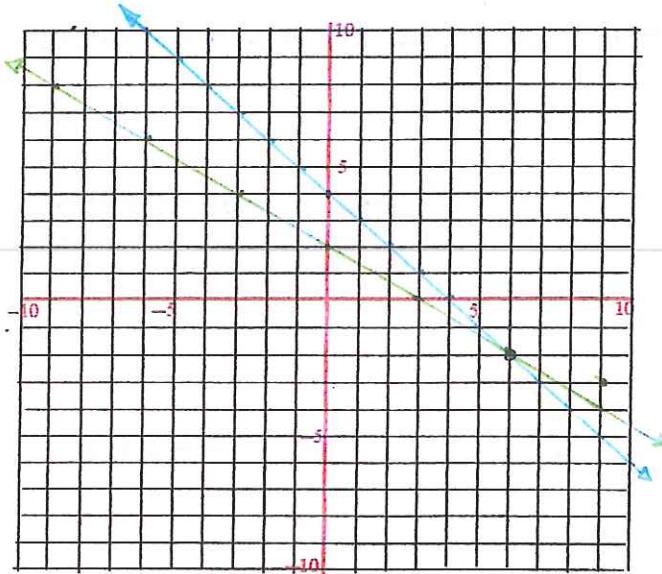


INFINITELY MANY SOLUTIONS



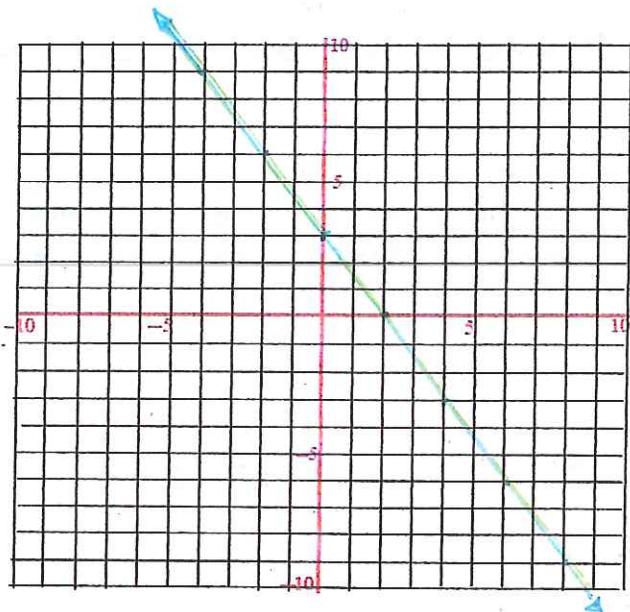
Graph each system of equations. Then determine the solution of the system.

4. $\begin{array}{l} 2x+3y=9 \rightarrow y = -\frac{2}{3}x + 3 \\ x+y=4 \rightarrow y = -x+4 \end{array}$



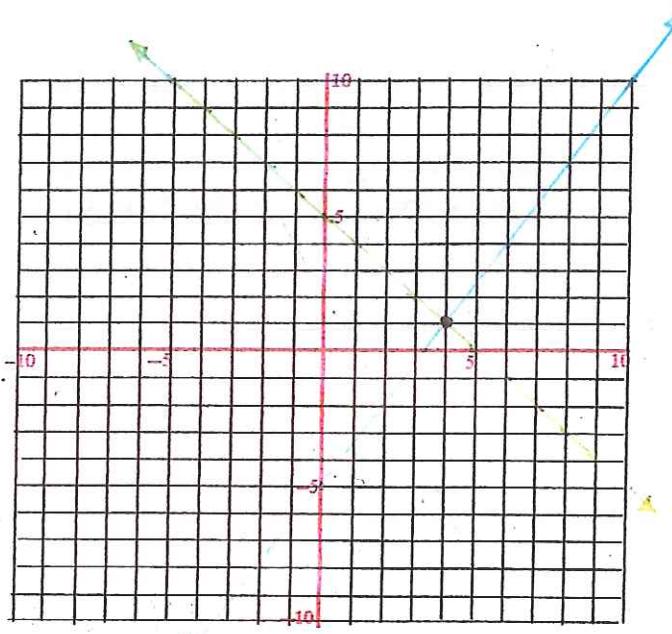
Solution: (6, -2)

5. $\begin{array}{l} 2y+3x=6 \rightarrow y = -\frac{3}{2}x + 3 \\ 4y+6x=12 \rightarrow y = -\frac{3}{2}x + 3 \end{array}$



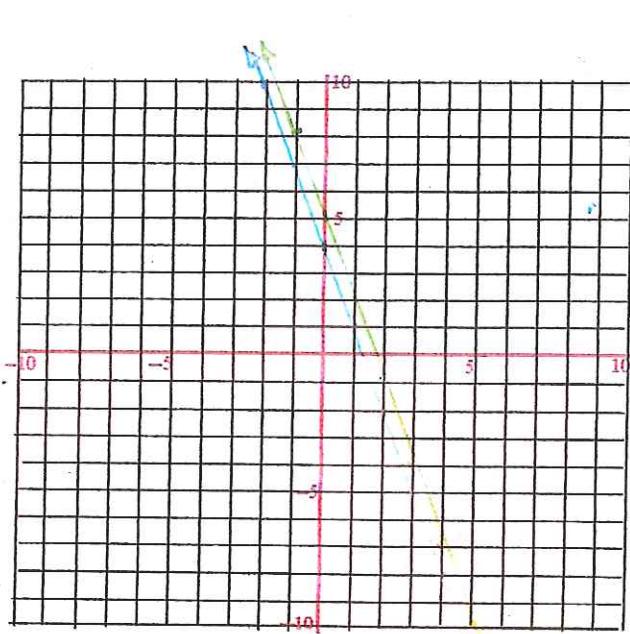
Solution: INFINITELY MANY SOLUTIONS

6. $\begin{array}{l} x+y=5 \rightarrow y = -x+5 \\ 3x-2y=10 \end{array}$



Solution: (4, 1)

7. $\begin{array}{l} y=-3x+5 \\ 9x+3y=12 \rightarrow y = -3x+4 \end{array}$



Solution: NO SOLUTION

$\vee \wedge$

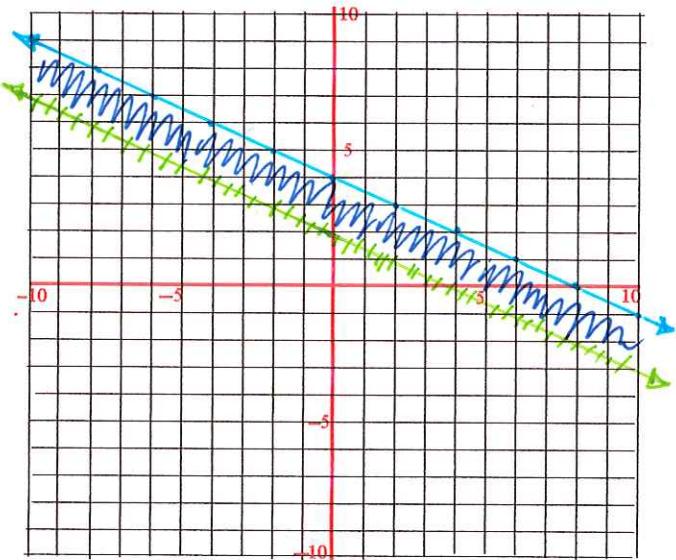
Dashed Line (No Inclusion)

System of Inequalities

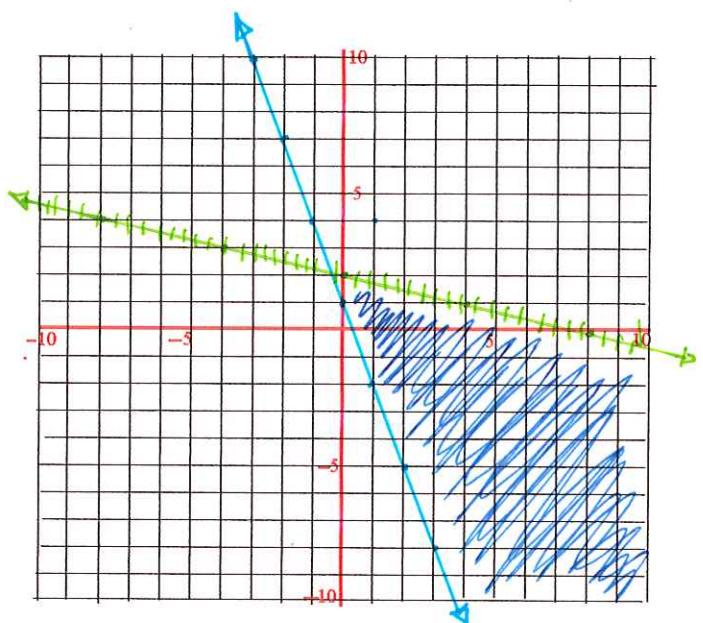
$\vee \wedge$

Solid Line (Inclusion)

8.) $\begin{cases} 3x + 6y - 12 > 0 \\ x + 2y \leq 8 \end{cases} \rightarrow \begin{cases} y > -\frac{1}{2}x + 2 \\ y \leq -\frac{1}{2}x + 4 \end{cases}$



9.) $\begin{cases} 8 > 4y + x \\ 8y \geq -24x + 8 \end{cases} \rightarrow \begin{cases} y < -\frac{1}{4}x + 2 \\ y \geq -3x + 1 \end{cases}$



10.) $\begin{cases} -x + 3y < 6 \\ 2x - y < 8 \end{cases} \rightarrow \begin{cases} y < \frac{1}{3}x + 2 \\ y > 2x - 8 \end{cases}$

